

Name: _____ Date: _____

Solving Exponential Functions

Solve each equation:

1. $8^{2x-5} = 8^{x+3}$

$$\begin{array}{r} 2x-5 = x+3 \\ -x \quad -x \\ \hline x-5 = 3 \\ +5 \quad +5 \\ \hline x = 8 \end{array}$$

2. $9^{x-5} = 27$

$$x = \frac{13}{2}$$

3. $5^{2x+3} = 625$

$$\begin{array}{r} 2x+3 = 4 \\ -3 \quad -3 \\ \hline 2x = 1 \\ \frac{2x}{2} = \frac{1}{2} \\ \hline x = \frac{1}{2} \end{array}$$

$625 = 5^4$
 \uparrow
 125
 \uparrow
 25
 \uparrow
 5

4. $9^x = 27^{2x+8}$

$$x = -6$$

5. $3^{2x+3} = 27^{x+1}$

$$\begin{array}{r} 2x+3 = 3(x+1) \\ 2x+3 = 3x+3 \\ -3x \quad -3x \\ \hline -x+3 = 3 \\ +3 \quad +3 \\ \hline -x = 0 \\ \frac{-x}{-1} = \frac{0}{-1} \\ \hline x = 0 \end{array}$$

$27 = 3^3$
 \uparrow
 9
 \uparrow
 3

6. $125^x = 25^{x+1}$

$$x = 2$$

7. $4^{3x} = 8^{x+1}$

$4 = 2^2$ $8 = 2^3$

$$\begin{array}{r} (2^2)^{3x} = (2^3)^{x+1} \\ 6x = 3x+3 \\ -3x \quad -3x \\ \hline 3x = 3 \\ \frac{3x}{3} = \frac{3}{3} \\ \hline x = 1 \end{array}$$

8. $4^x + 5 = 21$

$$x = 2$$

9. $3^{x-14} = \left(\frac{1}{3}\right)^{2x-1}$

$\frac{1}{3} = 3^{-1}$

$$\begin{array}{r} 3^{x-14} = (3^{-1})^{2x-1} \\ x-14 = -2x+1 \\ +2x \quad +2x \\ \hline 3x-14 = 1 \\ +14 \quad +14 \\ \hline 3x = 15 \\ \frac{3x}{3} = \frac{15}{3} \\ \hline x = 5 \end{array}$$

10. $81^{x+3} = \left(\frac{1}{3}\right)^{5x-6}$

$x = -\frac{2}{3}$

11. $\left(\frac{1}{3}\right)^x = 18$ $\frac{1}{3} = 3^{-1}$
 $\frac{-1}{-1} = \frac{18}{-1}$
 $27 = 3^3$

$\left(\frac{1}{3}\right)^x = 27$

$(3^{-1})^x = 3^3$

$3^{-x} = 3^3$

$\frac{-x}{-1} = \frac{3}{-1}$

$x = -3$

12. $4^x = \left(\frac{1}{2}\right)^{x-3}$

$x = 1$

Solve each inequality:

13. $4^{3x} < 2^{x+10}$ $4 = 2^2$
 $(2^2)^{3x} < 2^{x+10}$
 $2^{6x} < 2^{x+10}$

$6x < x+10$

$\frac{5x < 10}{5 \quad 5}$

$x < 2$

14. $3^x \leq 27^{x-4}$

$x \geq 6$

15. $7^{7x-6} > 7^{5x+2}$

$7x-6 > 5x+2$

$\frac{-5x > 8}{-5x \quad -5x}$

$2x-6 > 2$
 $+6 \quad +6$

$\frac{2x > 8}{2 \quad 2}$

$x > 4$

16. Solve each exponential equation. Identify the property of equality that allows you to carry out each step.

** Go Back to Unit 3 to help **

Equation	Steps
$3^x - 9 = 72$	Given

17. There are 8 bacteria in a culture. The number of bacteria in the culture quadruples every hour. After how many hours will there be 2,048 bacteria?

$y = ab^x$

$\frac{2048}{8} = \frac{8(4)^x}{8}$

$256 = (4)^x$

$4^4 = (4)^x$

$4 = x$

4 hours